

Walter's original email about the pcal extraction algorithm is copied in below.

There are also a couple of old documents from Sergei Pogrebenko which detail it [EVN Doc 2 EVN Doc 8](#)

A key parameter is the greatest common factor of the sample frequency and the frequency offset. This number leads to a number I will call N that tells you how many baseband data samples are required before the phase cal time series repeats itself exactly yielding the same phase.

The algorithm I envision works as follows:

1. create a real-valued accumulator array, A, with dimension N.
2. for the duration of an accumulation period, fold the voltage data, V, into this array:

```
for(i = 0; i < nsamples; i++) A[i % N] += V[i]
```

3. Perform a real-to-complex Fourier transform on this array into an N/2 element complex array B

$$B = \text{FFT}[A]$$

4. Extract the tones wanted. The B array has N/2 points, but one will only be interested in a very small subset of those points - the ones that correspond to the pulse cal tone frequencies. Note that it might be faster to do a DFT only for the desired points rather than performing a full FFT to generate the entire spectrum.

As a concrete example, let's consider the VLBI case with a single baseband channel, bandwidth $bw = 2^n$ MHz, with 1 tone per MHz, with the first tone $\nu = 10 \cdot d$ kHz offset from the DC edge of the channel for integer d (note this is a standard case for VLBI).

The condition for return-to-phase is:

$$\Delta \phi = 2\pi \nu \Delta T = R \cdot 2\pi \text{ for integer } R$$

ΔT must be an integral number of samples which we call N (the same N as above). Each sample is $2^{-(n-1)}$ microseconds in duration. Thus

$$d/100 \text{ MHz} \cdot N \cdot 2^{-(n-1)} \text{ mus} = R$$

or

$$d \cdot N = 200 \cdot 2^n \cdot R$$

This expression is where the greatest common divisor concept comes in. It is easy to see that $N = 200 \cdot 2^n$ will meet the required condition for all values of d, meaning for all possible tones in the baseband. For 8 MHz this implies $N = 1600$ points which forms a spectrum with 800 complex points. There will be 8 tones to recover, each separated by 1 MHz = 100 points in the spectrum. The position of the first tone is at spectrum bin $800 \cdot \nu / bw$. The remaining 792 points of the spectrum are to be discarded.

Note the key aspect of this is that all of the averaging is done in the time domain and a single transform to the frequency domain is needed. There might be some logistical reason for doing the FFT and tone selection once per sub-integration in order to minimize data transfer from core processes to the manager process.

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