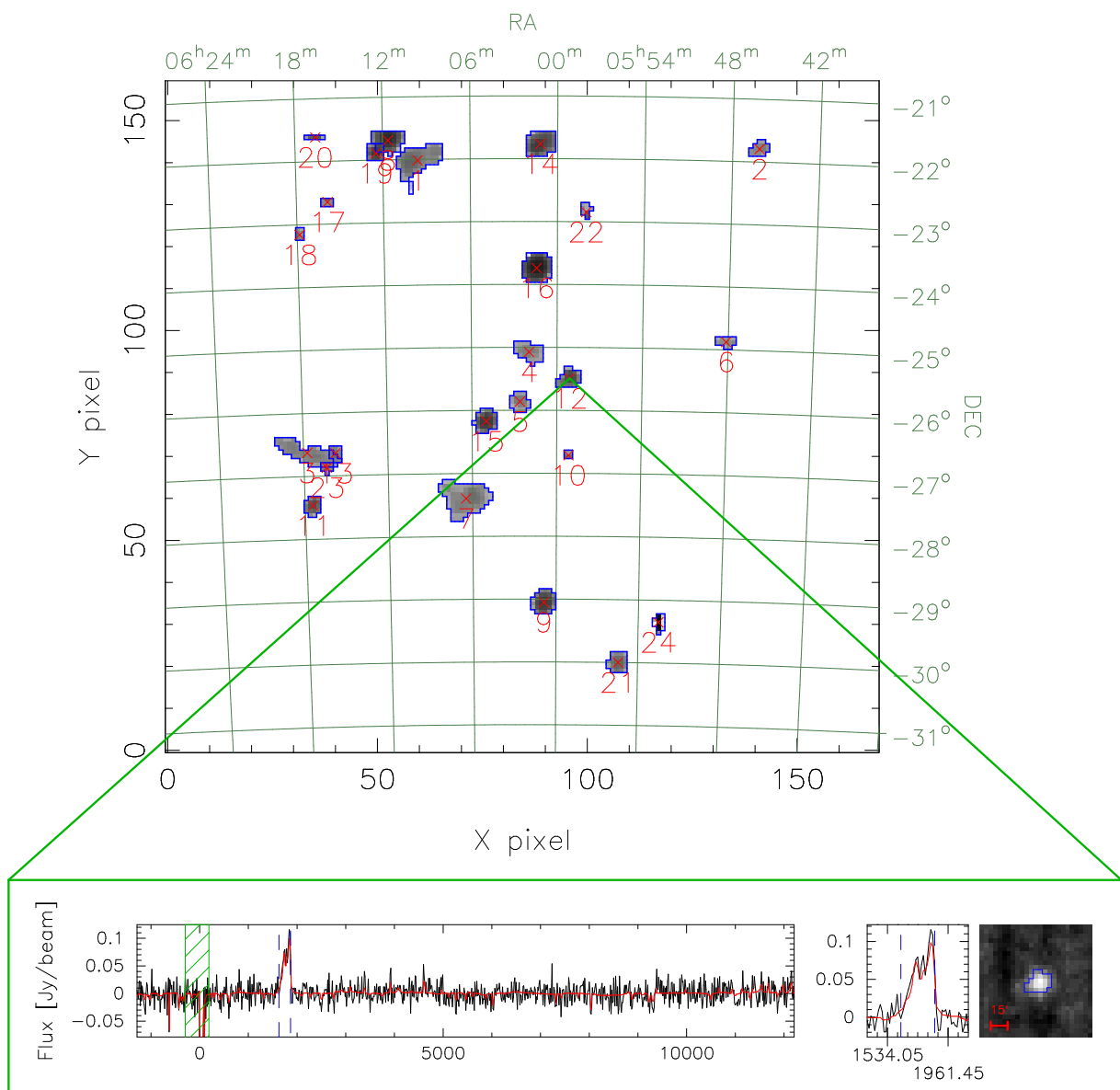


Source Detection with *Duchamp* v1.0

A User's Guide

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1 Introduction and getting going quickly

This document provides a user's guide to *Duchamp*, an object-finder for use on spectral-line data cubes. The basic execution of *Duchamp* is to read in a FITS data cube, find sources in the cube, and produce a text file of positions, velocities and fluxes of the detections, as well as a postscript file of the spectra of each detection.

So, you have a FITS cube, and you want to find the sources in it. What do you do? The first step is to make an input file that contains the list of parameters. Brief and detailed examples are shown in Appendix C. This file provides the input file name, the various output files, and defines various parameters that control the execution.

The standard way to run *Duchamp* is by the command

```
Duchamp -p [parameter file]
```

replacing [parameter file] with the name of the file listing the parameters. Alternatively, you can use the syntax

```
Duchamp -f [FITS file]
```

where [FITS file] is the file you wish to search. In the latter case, all parameters will take their default values detailed in Appendix B. In either case, the program will then work away and give you the list of detections and their spectra. The program execution is summarised below, and detailed in §3. Information on inputs is in §2 and Appendix B, and descriptions of the output is in §4.

1.1 A summary of the execution steps

The basic flow of the program is summarised here – all steps are discussed in more detail in the following sections.

1. If the `-p` option is used, the parameter file given on the command line is read in, and the parameters absorbed.
2. The FITS image is located and read in to memory.
3. If requested, a FITS image with a previously reconstructed array is read in.
4. If requested, blank pixels are trimmed from the edges, and the baseline of each spectrum is removed.
5. If the reconstruction method is requested, and the reconstructed array has not been read in at Step 3 above, the cube is reconstructed using the *à trous* wavelet method.
6. Searching for objects then takes place, using the requested thresholding method.
7. The list of objects is condensed by merging neighbouring objects and removing those deemed unacceptable.
8. The baselines and trimmed pixels are replaced prior to output.
9. The details of the detections are written to screen and to the requested output file.
10. Maps showing the spatial location of the detections are written.

11. The integrated spectra of each detection are written to a postscript file.
12. If requested, the reconstructed array can be written to a new FITS file.

1.2 Guide to terminology

First, a brief note on the use of terminology in this guide. *Duchamp* is designed to work on FITS “cubes”. These are FITS¹ image arrays with three dimensions – they are assumed to have the following form: the first two dimensions (referred to as x and y) are spatial directions (that is, relating to the position on the sky), while the third dimension, z , is the spectral direction, which can correspond to frequency, wavelength, or velocity. The three dimensional analogue of pixels are “voxels”, or volume cells – a voxel is defined by a unique (x, y, z) location and has a unique flux or intensity value associated with it.

Each spatial pixel (a given (x, y) coordinate) can be said to be a single spectrum, while a slice through the cube perpendicular to the spectral direction at a given z -value is a single channel (the 2-D image is a channel map).

Detection involves locating a contiguous group of voxels with fluxes above a certain threshold. *Duchamp* makes no assumptions as to the size or shape of the detected features, other than having user-selected minimum size criteria.

Features that are detected are assumed to be positive. The user can choose to search for negative features by setting an input parameter – this inverts the cube prior to the search (see §3.5 for details).

Note that it is possible to run *Duchamp* on a two-dimensional image (i.e. one with no frequency or velocity information), or indeed a one-dimensional array, and many of the features of the program will work fine. The focus, however, is on object detection in three dimensions.

1.3 Why *Duchamp*?

Well, it’s important for a program to have a name, and the initial working title of *cubefind* was somewhat uninspiring. I wanted to avoid the classic astronomical approach of designing a cute acronym, and since it is designed to work on cubes, I looked at naming it after a cubist. *Picasso*, sadly, was already taken (Minchin 1999), so I settled on naming it after Marcel Duchamp, another cubist, but also one of the first artists to work with “found objects”.

2 User Inputs

Input to the program is provided by means of a parameter file. Parameters are listed in the file, followed by the value that should be assigned to them. The syntax used is `paramName value`. Parameter names are not case-sensitive, and lines in the input file that start with `#` are ignored. If a parameter is listed more than once, the latter value is used, but otherwise the order in which the parameters are listed in the input file is arbitrary.

If a parameter is not listed, the default value is assumed. The defaults are chosen to provide a good result (using the reconstruction method), so the user doesn’t need to

¹FITS is the Flexible Image Transport System – see Hanisch et al. (2001) or websites such as <http://fits.cv.nrao.edu/FITS.html> for details.

specify many new parameters in the input file. Note that the image file **must** be specified! The parameters that can be set are listed in Appendix B, with their default values in parentheses.

The parameters with names starting with `flag` are stored as `bool` variables, and so are either `true = 1` or `false = 0`. *Duchamp* will only read them from the file as integers, and so they should be entered in the file as 0 or 1 (see example file in Appendix C).

3 What *Duchamp* is doing

The execution flow of *Duchamp* is detailed here, indicating the main algorithmic steps that are used. The program is written in C/C++ and makes use of the CFITSIO, WCSLIB and PGPLOT libraries.

3.1 Image input

The cube is read in using basic CFITSIO commands, and stored as an array in a special C++ class. This class keeps track of the list of detected objects, as well as any reconstructed arrays that are made (see §3.3). The World Coordinate System (WCS) information for the cube is also obtained from the FITS header by WCSLIB functions (Calabretta & Greisen 2002; Greisen & Calabretta 2002), and this information, in the form of a `wcsprm` structure, is also stored in the same class.

A sub-section of an image can be requested via the `subsection` parameter in the parameter file – this can be a good idea if the cube has very noisy edges, which may produce many spurious detections. The generalised form of the subsection that is used by CFITSIO is `[x1:x2:dx,y1:y2:dy,z1:z2:dz]`, such that the x-coordinates run from `x1` to `x2` (inclusive), with steps of `dx`. The step value can be omitted (so a subsection of the form `[2:50,2:50,10:1000]` is still valid). *Duchamp* does not make use of any step value present in the subsection string, and any that are present are removed before the file is opened.

If one wants the full range of a coordinate then replace the range with an asterisk, e.g. `[2:50,2:50,*]`. If one wants to use a subsection, one must set `flagSubsection = 1`. A complete description of the section syntax can be found at the FITSIO web site ².

3.2 Image modification

Several modifications to the cube can be made that improve the execution and efficiency of *Duchamp* (these are optional – their use is indicated by the relevant flags set in the input parameter file).

3.2.1 Blank pixel removal

First, the cube is trimmed of any BLANK pixels that pad the image out to a rectangular shape. This is optional, its use determined by the `flagBlankPix` parameter. The value for these pixels is read from the FITS header (using the BLANK, BSCALE and BZERO keywords), but if these are not present then the value can be specified by the user in the parameter file using `blankPixValue`.

² <http://heasarc.gsfc.nasa.gov/docs/software/fitsio/c/c.user/node90.html>

This stage is particularly important for the reconstruction step, as lots of BLANK pixels on the edges will smooth out features in the wavelet calculation stage. The trimming will also reduce the size of the cube’s array, speeding up the execution. The amount of trimming is recorded, and these pixels are added back in once the source-detection is completed (so that quoted pixel positions are applicable to the original cube).

Rows and columns are trimmed one at a time until the first non-BLANK pixel is reached, so that the image remains rectangular. In practice, this means that there will be BLANK pixels left in the trimmed image (if the non-BLANK region is non-rectangular). However, these are ignored in all further calculations done on the cube.

3.2.2 Baseline removal

Second, the user may request the removal of baselines from the spectra, via the parameter `flagBaseline`. This may be necessary if there is a strong baseline ripple present, which can result in spurious detections at the high points of the ripple. The baseline is calculated from a wavelet reconstruction procedure (see §3.3) that keeps only the two largest scales. This is done separately for each spatial pixel (i.e. for each spectrum in the cube), and the baselines are stored and added back in before any output is done. In this way the quoted fluxes and displayed spectra are as one would see from the input cube itself – even though the detection (and reconstruction if applicable) is done on the baseline-removed cube.

The presence of very strong signals (for instance, masers at several hundred Jy) can affect the determination of the baseline, leading to a large dip centred on the signal in the baseline-subtracted spectrum. To prevent this, the signal is trimmed prior to the reconstruction process at some standard threshold (at 8σ above the mean). The baseline determined should thus be representative of the true, signal-free baseline. Note that this trimming is only a temporary measure which does not affect the source-detection.

3.2.3 Ignoring bright Milky Way emission

Finally, a single set of contiguous channels can be ignored – these may exhibit very strong emission, such as that from the Milky Way as seen in extragalactic HI cubes (hence the references to “Milky Way” in relation to this task – apologies to Galactic astronomers!). Such dominant channels will produce many detections that are unnecessary, uninteresting (if one is interested in extragalactic HI) and large (in size and hence in memory usage), and so will slow the program down and detract from the interesting detections. The use of this feature is controlled by the `flagMW` parameter, and the exact channels concerned are able to be set by the user (using `maxMW` and `minMW` – these give an inclusive range of channels). When employed, these channels are temporarily blanked out for the searching, and the scaling of the spectral output (see Fig. 1) will not take them into account. They will be present in the reconstructed array, however, and so will be included in the saved FITS file (see §3.4). When the final spectra are plotted, the range of channels covered by these parameters is indicated by a green hashed box.

3.3 Image reconstruction

The user can direct *Duchamp* to reconstruct the data cube using the *à trous* wavelet procedure. A good description of the procedure can be found in Starck & Murtagh (2002). The reconstruction is an effective way of removing a lot of the noise in the image, allowing one to search reliably to fainter levels, and reducing the number of spurious detections.

This is an optional step, but one that greatly enhances the source-detection process, with the payoff that it can be relatively time- and memory-intensive.

3.3.1 Algorithm

The steps in the *à trous* reconstruction are as follows:

1. Set the reconstructed array to 0 everywhere.
2. The input array is discretely convolved with a given filter function. This is determined from the parameter file via the `filterCode` parameter – see Appendix B for details on the filters available.
3. The wavelet coefficients are calculated by taking the difference between the convolved array and the input array.
4. If the wavelet coefficients at a given point are above the requested threshold (given by `snrRecon` as the number of σ above the mean and adjusted to the current scale – see Appendix H), add these to the reconstructed array.
5. The separation of the filter coefficients is doubled. (Note that this step provides the name of the procedure³, as gaps or holes are created in the filter coverage.)
6. The procedure is repeated from step 2, using the convolved array as the input array.
7. Continue until the required maximum number of scales is reached.
8. Add the final smoothed (i.e. convolved) array to the reconstructed array. This provides the “DC offset”, as each of the wavelet coefficient arrays will have zero mean.

The reconstruction has at least two iterations. The first iteration makes a first pass at the wavelet reconstruction (the process outlined in the 8 stages above), but the residual array will inevitably have some structure still in it, so the wavelet filtering is done on the residual, and any significant wavelet terms are added to the final reconstruction. This step is repeated until the change in the σ of the background is less than some fiducial amount.

It is important to note that the *à trous* decomposition is an example of a “redundant” transformation. If no thresholding is performed, the sum of all the wavelet coefficient arrays and the final smoothed array is identical to the input array. The thresholding thus removes only the unwanted structure in the array.

Note that any BLANK pixels that are still in the cube will not be altered by the reconstruction – they will be left as BLANK so that the shape of the valid part of the cube is preserved.

3.3.2 Note on Statistics

The correct calculation of the reconstructed array needs good estimation of the underlying mean and standard deviation of the background noise distribution. These statistics are estimated using robust methods, to avoid corruption by strong outlying points. The mean of the distribution is actually estimated by the median, while the median absolute deviation from the median (MADFM) is calculated and corrected assuming Gaussianity to

³*à trous* means “with holes” in French.

estimate the underlying standard deviation σ . The Gaussianity (or Normality) assumption is critical, as the MADFM does not give the same value as the usual rms or standard deviation value – for a normal distribution $N(\mu, \sigma)$ we find $\text{MADFM} = 0.6744888\sigma$. The difference between the MADFM and σ is corrected for, so the user need only think in the usual multiples of σ when setting `snrRecon`. See Appendix G for a derivation of this value.

When thresholding the different wavelet scales, the value of σ as measured from the wavelet array needs to be scaled to account for the increased amount of correlation between neighbouring pixels (due to the convolution). See Appendix H for details on this scaling.

3.3.3 User control of reconstruction parameters

The most important parameter for the user to select in relation to the reconstruction is the threshold for each wavelet array. This is set using the `snrRecon` parameter, and is given as a multiple of the rms (estimated by the MADFM) above the mean (which for the wavelet arrays should be approximately zero). There are several other parameters that can be altered as well that affect the outcome of the reconstruction.

By default, the cube is reconstructed in three dimensions, using a 3-dimensional filter and 3-dimensional convolution. This can be altered, however, using the parameter `reconDim`. If set to 1, this means the cube is reconstructed by considering each spectrum separately, whereas `reconDim=2` will mean the cube is reconstructed by doing each channel map separately. The merits of these choices are discussed in §5, but it should be noted that a 2-dimensional reconstruction can be susceptible to edge effects if the spatial shape is not rectangular.

The user can also select the minimum scale to be used in the reconstruction – the first scale exhibits the highest frequency variations, and so ignoring this one can sometimes be beneficial in removing excess noise. The default, however, is to use all scales (`minscale = 1`).

Finally, the filter that is used for the convolution can be selected by using `filterCode` and the relevant code number – the choices are listed in Appendix B. A larger filter will give a better reconstruction, but take longer and use more memory when executing. When multi-dimensional reconstruction is selected, this filter is used to construct a 2- or 3-dimensional equivalent.

3.4 Reconstruction I/O

The reconstruction stage can be relatively time-consuming, particularly for large cubes and reconstructions in 3-D. To get around this, *Duchamp* provides a shortcut to allow users to perform multiple searches (e.g. with different thresholds) on the same reconstruction without calculating the reconstruction each time.

The first step is to choose to save the reconstructed array as a FITS file by setting `flagOutputRecon = true`. The file will be saved in the same directory as the input image, so the user needs to have write permissions for that directory.

The filename will be derived from the input filename, with extra information detailing the reconstruction that has been done. For example, suppose `image.fits` has been reconstructed using a 3-dimensional reconstruction with filter 2, thresholded at 4σ using all scales. The output filename will then be `image.RECON-3-2-4-1.fits` (i.e. it uses the four parameters relevant for the *à trous* reconstruction as listed in Appendix B).

The new FITS file will also have these parameters as header keywords. If a subsection of the input image has been used (see §3.1), the format of the output filename will be `image.sub.RECON-3-2-4-1.fits`, and the subsection that has been used is also stored in the FITS header.

Likewise, the residual image, defined as the difference between the input and reconstructed arrays, can also be saved in the same manner by setting `flagOutputResid = true`. Its filename will be the same as above, with `RESID` replacing `RECON`.

If a reconstructed image has been saved, it can be read in and used instead of redoing the reconstruction. To do so, the user should set `flagReconExists = true`. The user can indicate the name of the reconstructed FITS file using the `reconFile` parameter, or, if this is not specified, *Duchamp* searches for the file with the name as defined above. If the file is not found, the reconstruction is performed as normal. Note that to do this, the user needs to set `flagAtrous = true` (obviously, if this is `false`, the reconstruction is not needed).

3.5 Searching the image

The image is searched for detections in two ways: spectrally (a 1-dimensional search in the spectrum in each spatial pixel), and spatially (a 2-dimensional search in the spatial image in each channel). In both cases, the algorithm finds connected pixels that are above the user-specified threshold. In the case of the spatial image search, the algorithm of [Lutz \(1980\)](#) is used to raster scan through the image and connect groups of pixels on neighbouring rows.

Note that this algorithm cannot be applied directly to a 3-dimensional case, as it requires that objects are completely nested in a row: that is, if you are scanning along a row, and one object finishes and another starts, you know that you will not get back to the first one (if at all) until the second is completely finished for that row. Three-dimensional data does not have this property, which is why we break up the searching into 1- and 2-dimensional cases.

The determination of the threshold is done in one of two ways. The first way is a simple sigma-clipping, where a threshold is set at a fixed number n of standard deviations above the mean, and pixels above this threshold are flagged as detected. The value of n is set with the parameter `snrCut`. As before, the value of the standard deviation is estimated by the MADFM, and corrected by the ratio derived in Appendix G.

The second method uses the False Discovery Rate (FDR) technique ([Hopkins et al. 2002](#); [Miller et al. 2001](#)), whose basis we briefly detail here. The false discovery rate (given by the number of false detections divided by the total number of detections) is fixed at a certain value α (e.g. $\alpha = 0.05$ implies 5% of detections are false positives). In practice, an α value is chosen, and the ensemble average FDR (i.e. $\langle FDR \rangle$) when the method is used will be less than α . One calculates p – the probability, assuming the null hypothesis is true, of obtaining a test statistic as extreme as the pixel value (the observed test statistic) – for each pixel, and sorts them in increasing order. One then calculates d where

$$d = \max_j \left\{ j : P_j < \frac{j\alpha}{c_N N} \right\},$$

and then rejects all hypotheses whose p -values are less than or equal to P_d . (So a $P_i < P_d$ will be rejected even if $P_i \geq j\alpha/c_N N$.) Note that “reject hypothesis” here means “accept

the pixel as an object pixel” (i.e. we are rejecting the null hypothesis that the pixel belongs to the background).

The c_N values here are normalisation constants that depend on the correlated nature of the pixel values. If all the pixels are uncorrelated, then $c_N = 1$. If N pixels are correlated, then their tests will be dependent on each other, and so $c_N = \sum_{i=1}^N i^{-1}$. Hopkins et al. (2002) consider real radio data, where the pixels are correlated over the beam. In this case the sum is made over the N pixels that make up the beam. The value of N is calculated from the FITS header (if the correct keywords – BMAJ, BMIN – are not present, a default value of 10 pixels is assumed).

The theory behind the FDR method implies a direct connection between the choice of α and the fraction of detections that will be false positives. However, due to the merging process, this direct connection is lost when looking at the final number of detections – see discussion in §5. The effect is that the number of false detections will be less than indicated by the α value used.

If a reconstruction has been made, the residuals (defined as original – reconstruction) are used to estimate the noise parameters of the cube. Otherwise they are estimated directly from the cube itself. In both cases, robust estimators are used as described above.

Detections must have a minimum number of pixels to be counted. This minimum number is given by the input parameters `minPix` (for 2-dimensional searches) and `minChannels` (for 1-dimensional searches).

The search only looks for positive features. If one is interested instead in negative features (such as absorption lines), set the parameter `flagNegative = true`. This will invert the cube (i.e. multiply all pixels by -1) prior to the search, and then re-invert the cube (and the fluxes of any detections) after searching is complete. All outputs are done in the same manner as normal, so that fluxes of detections will be negative.

3.6 Merging detected objects

The searching step produces a list of detected objects that will have many repeated detections of a given object – for instance, spectral detections in adjacent pixels of the same object and/or spatial detections in neighbouring channels. These are then combined in an algorithm that matches all objects judged to be “close”. This determination is made in one of two ways.

One way is to define two thresholds – one spatial and one in velocity – and say that two objects should be merged if there is at least one pair of pixels that lie within these threshold distances of each other. These thresholds are specified by the parameters `threshSpatial` and `threshVelocity` (in units of pixels and channels respectively).

Alternatively, the spatial requirement can be changed to say that there must be a pair of pixels that are *adjacent* – a stricter, but perhaps more realistic requirement, particularly when the spatial pixels have a large angular size (as is the case for HI surveys). This method can be selected by setting the parameter `flagAdjacent` to 1 (i.e. `true`) in the parameter file. The velocity thresholding is done in the same way as the first option.

Once the detections have been merged, they may be “grown”. This is a process of increasing the size of the detection by adding adjacent pixels that are above some secondary threshold. This threshold is lower than the one used for the initial detection, but above the noise level, so that faint pixels are only detected when they are close to a bright pixel. The value of this threshold is a possible input parameter (`growthCut`), with a default value of 1.5σ . The use of the growth algorithm is controlled by the `flagGrowth` parameter –

the default value of which is `false`. If the detections are grown, they are sent through the merging algorithm a second time, to pick up any detections that now overlap or have grown over each other.

Finally, to be accepted, the detections must span *both* a minimum number of channels (to remove any spurious single-channel spikes that may be present), and a minimum number of spatial pixels. These numbers, as for the original detection step, are set with the `minChannels` and `minPix` parameters. The channel requirement means there must be at least one set of `minChannels` consecutive channels in the source for it to be accepted.

4 Outputs

4.1 During execution

Duchamp provides the user with feedback whilst it is running, to keep the user informed on the progress of the analysis. Most of this consists of self-explanatory messages about the particular stage the program is up to. The relevant parameters are printed to the screen at the start (once the file has been successfully read in), so the user is able to make a quick check that the setup is correct (see Appendix `app-input` for an example).

If the cube is being trimmed (§3.2), the resulting dimensions are printed to indicate how much has been trimmed. If a reconstruction is being done, a continually updating message shows either the current iteration and scale, compared to the maximum scale (when `reconDim=3`), or a progress bar showing the amount of the cube that has been reconstructed (for smaller values of `reconDim`).

During the searching algorithms, the progress through the 1D and 2D searches are shown. When the searches have completed, the number of objects found in both the 1D and 2D searches are reported (see §3.5 for details).

In the merging process (where multiple detections of the same object are combined – see §3.6), two stages of output occur. The first is when each object in the list is compared with all others. The output shows two numbers: the first being how far through the list the current object is, and the second being the length of the list. As the algorithm proceeds, the first number should increase and the second should decrease (as objects are combined). When the numbers meet (i.e. the whole list has been compared), the second phase begins, in which multiply-appearing pixels in each object are removed, as are objects not meeting the minimum channels requirement. During this phase, the total number of accepted objects is shown, which should steadily increase until all have been accepted or rejected. Note that these steps can be very quick for small numbers of detections.

Since this continual printing to screen has some overhead of time and CPU involved, the user can elect to not print this information by setting the parameter `verbose = 0`. In this case, the user is still informed as to the steps being undertaken, but the details of the progress are not shown.

4.2 Results

4.2.1 Table of Results

Finally, we get to the results – the reason for running *Duchamp* in the first place. Once the detection list is finalised, it is sorted by the mean velocity of the detections (or, if there is no good WCS associated with the cube, by the mean Z-pixel position). The results

are then printed to the screen and to the output file, given by the `OutFile` parameter. The results list, an example of which can be seen in Appendix D, contains the following columns (note that the title of the columns depending on WCS information will depend on the projection of the WCS):

Obj#:	The ID number of the detection (simply the sequential count for the list, which is ordered by increasing velocity).
Name:	The IAU-format name of the detection (derived from the WCS projection).
X:	The average X-pixel position.
Y:	The average Y-pixel position.
Z:	The average Z-pixel position.
RA/GLON:	The Right Ascension or Galactic Longitude of the centre of the object.
DEC/GLAT:	The Declination or Galactic Latitude of the centre of the object.
VEL:	The mean velocity of the object [units given by the <code>spectralUnits</code> parameter].
w_RA/w_GLON:	The width of the object in Right Ascension or Galactic Longitude [arcmin].
w_DEC/w_GLAT:	The width of the object in Declination Galactic Latitude [arcmin].
w_VEL:	The full velocity width of the detection (max channel – min channel, in velocity units [see note below]).
F_int:	The integrated flux over the object, in the units of flux times velocity, corrected for the beam if necessary.
F_peak:	The peak flux over the object, in the units of flux.
X1, X2:	The minimum and maximum X-pixel coordinates.
Y1, Y2:	The minimum and maximum Y-pixel coordinates.
Z1, Z2:	The minimum and maximum Z-pixel coordinates.
Npix:	The number of voxels (i.e. distinct (x, y, z) coordinates) in the detection.
Flag:	Whether the detection has any warning flags (see below).

The Name is derived from the WCS position. For instance, a source centred on the RA,Dec position $12^h53^m45^s$, $-36^\circ24'12''$ will be called J125345–362412 (if the epoch is J2000) or B125345–362412 (if B1950). An alternative form is used for Galactic coordinates: a source centred on the position $(l,b) = (323.1245, 5.4567)$ will be called G323.124+05.457. If the WCS is not valid (i.e. is not present or does not have all the necessary information), the Name, RA, DEC, VEL and related columns are not printed, but the pixel coordinates are still provided.

The velocity units can be specified by the user, using the parameter `spectralUnits` (enter it as a single string). The default value is km/s, which should be suitable for most users. These units are also used to give the units of integrated flux.

The last column contains any warning flags about the detection. There are currently two options here. An ‘E’ is printed if the detection is next to the edge of the image, meaning either the limit of the pixels, or the limit of the non-BLANK pixel region. An

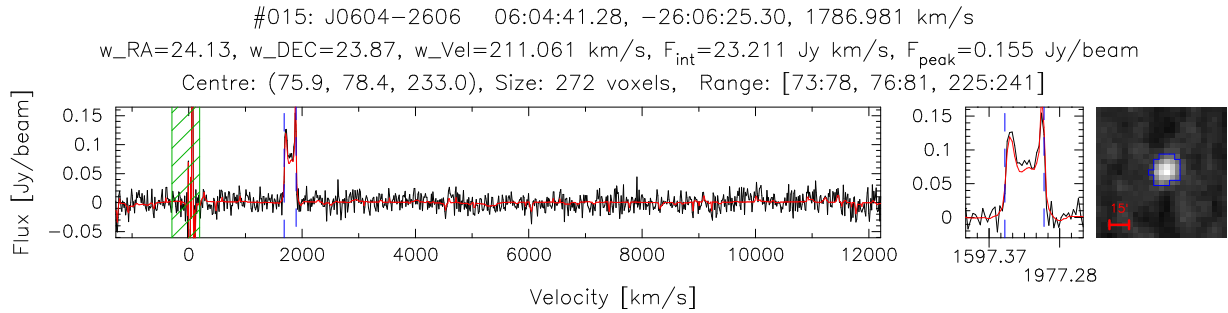


Figure 1: An example of the spectrum output. Note several of the features discussed in the text: the red lines indicating the reconstructed spectrum; the blue dashed lines indicating the spectral extent of the detection; the green hashed area indicating the Milky Way channels that are ignored by the searching algorithm; the blue border showing its spatial extent on the 0th moment map; and the 15 arcmin-long scale bar.

‘N’ is printed if the total flux, summed over all the (non-BLANK) pixels in the smallest box that completely encloses the detection, is negative. Note that this sum is likely to include non-detected pixels. It is of use in pointing out detections that lie next to strongly negative pixels, such as might arise due to interference – the detected pixels might then also be due to the interference, so caution is advised.

4.2.2 Other results lists

Two alternative results files can also be requested. One option is a VOTable-format XML file, containing just the RA, Dec, Velocity and the corresponding widths of the detections, as well as the fluxes. The user should set `flagVOT = 1`, and put the desired filename in the parameter `votFile` – note that the default is for it not to be produced. This file should be compatible with all Virtual Observatory tools (such as Aladin⁴). The second option is an annotation file for use with the Karma toolkit of visualisation tools (in particular, with `kvis`). This will draw a circle at the position of each detection, and number it according to the `Obj#` given above. To make use of this option, the user should set `flagKarma = 1`, and put the desired filename in the parameter `karmaFile` – again, the default is for it not to be produced.

As the program is running, it also (optionally) records the detections made in each individual spectrum or channel (see §3.5 for details on this process). This is recorded in the file given by the parameter `LogFile`. This file does not include the columns `Name`, `RA`, `DEC`, `w_RA`, `w_DEC`, `VEL`, `w_VEL`. This file is designed primarily for diagnostic purposes: e.g. to see if a given set of pixels is detected in, say, one channel image, but does not survive the merging process. The list of pixels (and their fluxes) in the final detection list are also printed to this file, again for diagnostic purposes. This feature can be turned off by setting `flagLog = false`. (This may be a good idea if you are not interested in its contents, as it can be a large file.)

4.2.3 Graphical output – spectra

As well as the output data file, a postscript file is created that shows the spectrum for each detection, together with a small cutout image (the 0th moment) and basic information

⁴ Aladin can be found on the web at <http://aladin.u-strasbg.fr/>

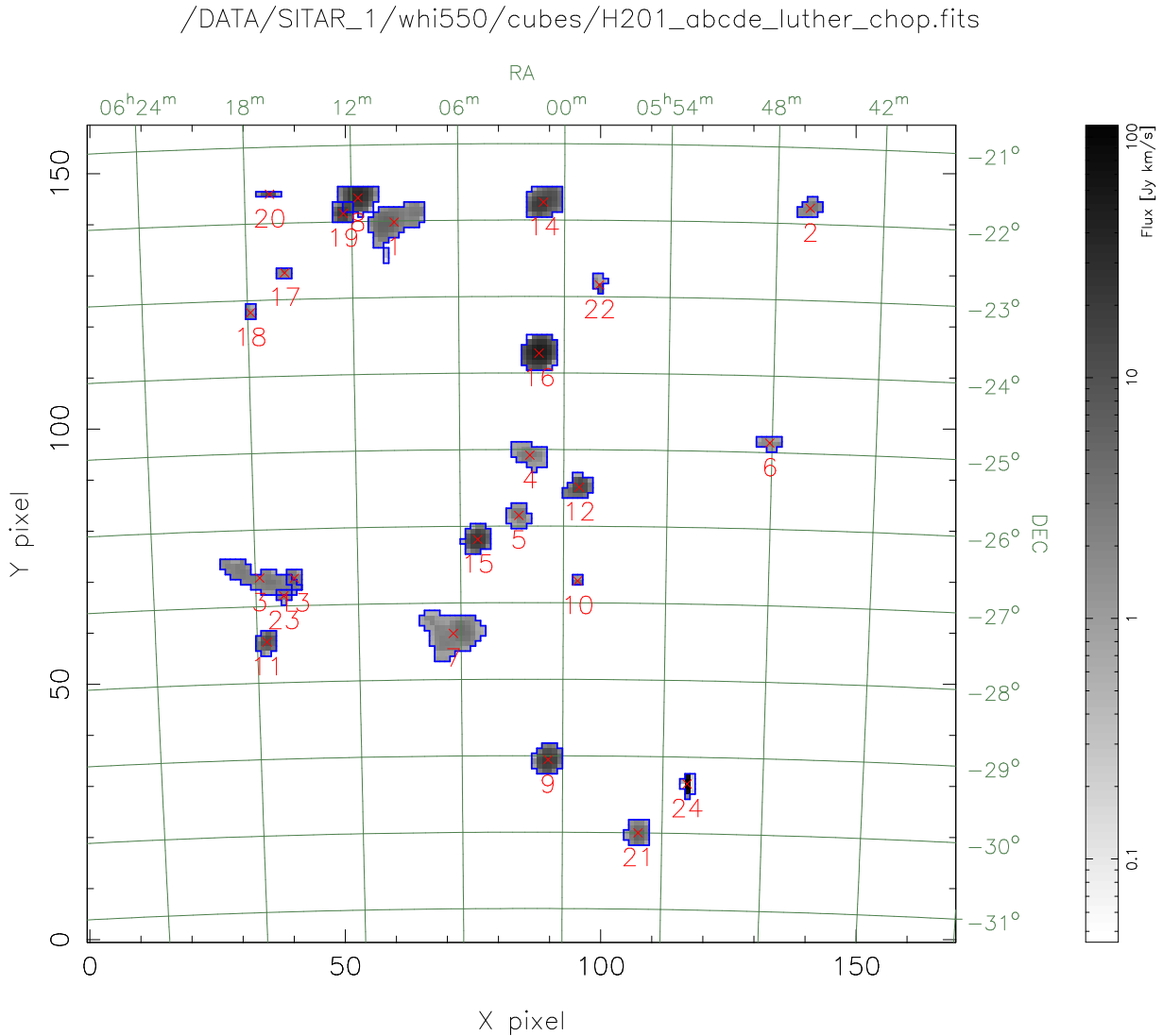


Figure 2: An example of the moment map created by *Duchamp*. The full extent of the cube is covered, and the 0th moment of each object is shown (integrated individually over all the detected channels).

about the detection (note that any flags are printed after the name of the detection, in the format [E]). If the cube was reconstructed, the spectrum from the reconstruction is shown in red, over the top of the original spectrum. The spectral extent of the detected object is indicated by two dashed blue lines, and the region covered by the “Milky Way” channels is shown by a green hashed box.

The spectrum that is plotted is governed by the `spectralMethod` parameter. It can be either `peak`, where the spectrum is from the spatial pixel containing the detection’s peak flux; or `sum`, where the spectrum is summed over all spatial pixels, and then corrected for the beam size.

The spectral extent of the detection is indicated with blue lines, and a zoom is shown in a separate window. The cutout image can optionally include a border around the spatial pixels that are in the detection (turned on and off by the parameter `drawBorders` – the default is `true`). It also includes a scale bar in the bottom left corner to indicate size – it is 15 arcmin long (note that due to projection effects it may be a slightly different physical length from object to object). An example detection can be seen below in Fig. 1.

4.2.4 Graphical output – maps

Finally, a couple of images are optionally produced: a 0th moment map of the cube, combining just the detected channels in each object, showing the integrated flux in grey-scale; and a “detection image”, a grey-scale image where the pixel values are the number of channels that spatial pixel is detected in. In both cases, if `drawBorders = true`, a border is drawn around the spatial extent of each detection. An example moment map is shown in Fig. 2. The production or otherwise of these images is governed by the `flagMaps` parameter.

The purpose of these images are to provide a visual guide to where the detections have been made, and, particularly in the case of the moment map, to provide an indication of the strength of the source. In both cases, the detections are numbered (in the same sense as the output list), and the spatial borders are marked out as for the cutout images in the spectra file. Both these images are saved as postscript files (given by the parameters `momentMap` and `detectionMap` respectively), with the latter also displayed in a PGPLOT window (regardless of the state of `flagMaps`).

5 Notes and hints on the use of *Duchamp*

In using *Duchamp*, the user has to make a number of decisions about the way the program runs. This section is designed to give the user some idea about what to choose.

The main choice is whether or not to use the wavelet reconstruction. The main benefits of this are the marked reduction in the noise level, leading to regularly-shaped detections, and good reliability for faint sources. The main drawback with its use is the long execution time: to reconstruct a $170 \times 160 \times 1024$ (HIPASS) cube often requires three iterations and takes about 20-25 minutes to run completely. Note that this is for the three-dimensional reconstruction: using `reconDim=1` makes the reconstruction quicker (the full program then takes about 6 minutes), but it is still the largest part of the time.

The searching part of the procedure is much quicker: searching an un-reconstructed cube leads to execution times of only a couple of minutes. Alternatively, using the ability to read in previously-saved reconstructed arrays makes running the reconstruction more than once a more feasible prospect.

On the positive side, the shape of the detections in a cube that has been reconstructed will be much more regular and smooth – the ragged edges that objects in the raw cube possess are smoothed by the removal of most of the noise. This enables better determination of the shapes and characteristics of objects.

A further point to consider when using the reconstruction is that if the two-dimensional reconstruction is chosen (`reconDim=2`), it can be susceptible to edge effects. If the valid area in the cube (i.e. the part that is not BLANK) has non-rectangular edges, the convolution can produce artefacts in the reconstruction that mimic the edges and can lead (depending on the selection threshold) to some spurious sources. Caution is advised with such data – the user is advised to check carefully the reconstructed cube for the presence of such artefacts. Note, however, that the 1- and 3-dimensional reconstructions are *not* susceptible in the same way, since the spectral direction does not generally exhibit these BLANK edges, and so we recommend the use of either of these.

If one chooses the reconstruction method, a further decision is required on the signal-to-noise cutoff used in determining acceptable wavelet coefficients. A larger value will remove more noise from the cube, at the expense of losing fainter sources, while a smaller

value will include more noise, which may produce spurious detections, but will be more sensitive to faint sources. Values of less than about 3σ tend to not reduce the noise a great deal and can lead to many spurious sources (although this will depend on the nature of the cube).

When it comes to searching, the FDR method produces more reliable results than simple sigma-clipping, particularly in the absence of reconstruction. However, it does not work in exactly the way one would expect for a given value of `alpha`. For instance, setting fairly liberal values of `alpha` (say, 0.1) will often lead to a much smaller fraction of false detections (i.e. much less than 10%). This is the effect of the merging algorithms, that combine the sources after the detection stage, and reject detections not meeting the minimum pixel or channel requirements. It is thus better to aim for larger `alpha` values than those derived from a straight conversion of the desired false detection rate.

Finally, as *Duchamp* is still undergoing development, there are some elements that are not fully developed. In particular, it is not as clever as I would like at avoiding interference. The ability to place requirements on the minimum number of channels and pixels partially circumvents this problem, but work is being done to make *Duchamp* smarter at rejecting signals that are clearly (to a human eye at least) interference. See the following section for further improvements that are planned.

6 Future Developments

This is both a list of planned improvements and a wish-list of features that would be nice to include (but are not planned in the immediate future). Let me know if there are items not on this list, or items on the list you would like prioritised.

- Better determination of the noise characteristics of spectral-line cubes, including understanding how the noise is generated and developing a model for it. **Planned.**
- Include more source analysis. Examples could be: shape information; measurements of HI mass; more variety of measurements of velocity width and profile. **Some planned.**
- Provide some indication of the significance of the detection (i.e. some S/N-like value). **Planned.**
- Improved ability to reject interference, possibly on the spectral shape of features. **Planned.**
- Ability to separate (de-blend) distinct sources that have been merged. **Planned.**
- Link to lists of possible counterparts (e.g. via NED/SIMBAD/other VO tools?). **Wish-list.**
- On-line web service interface, so a user can upload a cube and get back a source-list. **Wish-list.**
- Embed *Duchamp* in a GUI, to move away from the text-based interaction. **Wish-list.**

References

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A Obtaining and Installing *Duchamp*

The *Duchamp* web page can be found at the following location:

<http://www.atnf.csiro.au/people/Matthew.Whiting/Duchamp>

Here you can find a gzipped tar archive of the source code that can be downloaded and extracted, as well as this User's Guide in postscript and hyperlinked PDF formats.

Duchamp can be built on Unix systems by typing:

```
> ./configure
> make
> make clean (optional -- to remove the object files)
```

Run in this manner, `configure` should find all the necessary libraries, but if the above-mentioned libraries have been installed in non-standard locations, you can specify additional directories to look in. There are separate options for library files (eg. `libcpgplot.a`) and header files (eg. `cpgplot.h`).

For example, if `WCSLIB` had been installed in `/home/mduchamp/wcslib`, there are two libraries that are likely to be in separate subdirectories: `C/` and `pgsbox/`. Each subdirectory needs to be searched for library and header files, so one could build *Duchamp* by typing:

```
> ./configure \
LIBDIRS="/home/mduchamp/wcslib/C /home/mduchamp/wcslib/pgsbox" \
INCDIRS="/home/mduchamp/wcslib/C /home/mduchamp/wcslib/pgsbox"
```

And then just run `make` in the usual fashion:

```
> make
```

This will produce the executable *Duchamp*. There are two possible ways to run it. The first is:

```
> Duchamp -f [FITS file]
```

where `[FITS file]` is the file you wish to search. This method simply uses the default values of all parameters.

The second method allows some determination of the parameter values by the user. Type:

```
> Duchamp -p [parameter file]
```

where `[parameterFile]` is a file with the input parameters, including the name of the cube you want to search. There are two example input files included with the distribution. The smaller one, `InputExample`, shows the typical parameters one might want to set. The large one, `InputComplete`, lists all possible parameters that can be entered, and a brief description of them. To get going quickly, just replace the "your-file-here" in `InputExample` with your image name, and type

```
> Duchamp -p InputExample
```

The following appendices provide details on the individual parameters, and show examples of the output files that *Duchamp* produces.

B Available parameters

The full list of parameters that can be listed in the input file are given here. If not listed, they take the default value given in parentheses. Since the order of the parameters in the input file does not matter, they are grouped here in logical sections.

Input-output related

ImageFile (no default assumed): The filename of the data cube to be analysed.

flagSubsection [false]: A flag to indicate whether one wants a subsection of the requested image.

Subsection [[*,*,*]]: The requested subsection, which should be specified in the format `[x1:x2,y1:y2,z1:z2]`, where the limits are inclusive. If the full range of a dimension is required, use a `*`, e.g. if you want the full spectral range of a subsection of the image, use `[30:140,30:140,*]`.

flagReconExists [false]: A flag to indicate whether the reconstructed array has been saved by a previous run of *Duchamp*. If set true, the reconstructed array will be read from the file given by `reconFile`, rather than calculated directly.

reconFile (no default assumed): The FITS file that contains the reconstructed array. If `flagReconExists` is true and this parameter is not defined, the default file searched will be determined by the *à trous* parameters (see §3.3).

OutFile [duchamp-Results.txt]: The file containing the final list of detections. This also records the list of input parameters.

SpectraFile [duchamp-Spectra.ps]: The postscript file containing the resulting integrated spectra and images of the detections.

flagLog [true]: A flag to indicate whether intermediate detections should be logged.

LogFile [duchamp-Logfile.txt]: The file in which intermediate detections are logged. These are detections that have not been merged. This is primarily for use in debugging and diagnostic purposes – normal use of the program will probably not require this.

flagOutputRecon [false]: A flag to say whether or not to save the reconstructed cube as a FITS file. The filename will be derived from the `ImageFile` – the reconstruction of `image.fits` will be saved as `image.RECON?.fits`, where `?` stands for the value of `snrRecon` (see below).

flagOutputResid [false]: As for `flagOutputRecon`, but for the residual array – the difference between the original cube and the reconstructed cube. The filename will be `image.RESID?.fits`.

flagVOT [false]: A flag to say whether to create a VOTable file corresponding to the information in `outfile`. This will be an XML file in the Virtual Observatory VOTable format.

votFile [duchamp-Results.xml]: The VOTable file with the list of final detections. Some input parameters are also recorded.

- flagKarma** [false]: A flag to say whether to create a Karma annotation file corresponding to the information in `outfile`. This can be used as an overlay for the Karma programs such as `kvis`.
- karmaFile** [duchamp-Results.ann]: The Karma annotation file showing the list of final detections.
- flagMaps** [true]: A flag to say whether to save postscript files showing the 0th moment map of the whole cube (parameter `momentMap`) and the detection image (`detectionMap`).
- momentMap** [duchamp-MomentMap.ps]: A postscript file containing a map of the 0th moment of the detected sources, as well as pixel and WCS coordinates.
- detectionMap** [duchamp-DetectionMap.ps]: A postscript file showing each of the detected objects, coloured in greyscale by the number of channels spanned by each pixel. Also shows pixel and WCS coordinates.

Modifying the cube

- flagBlankPix** [true]: A flag to say whether to remove BLANK pixels from the analysis – these are pixels set to some particular value because they fall outside the imaged area.
- blankPixValue** [-8.00061]: The value of the BLANK pixels, if this information is not contained in the FITS header (the usual procedure is to obtain this value from the header information – in which case the value set by this parameter is ignored).
- flagMW** [false]: A flag to say whether to ignore channels contaminated by Milky Way (or other) emission – the searching algorithms will not look at these channels.
- maxMW** [112]: The maximum channel number containing “Milky Way” emission.
- minMW** [75]: The minimum channel number containing “Milky Way” emission. Note that the range specified by `maxMW` and `minMW` is inclusive.
- flagBaseline** [false]: A flag to say whether to remove the baseline from each spectrum in the cube for the purposes of reconstruction and detection.

Detection related

General detection

- flagNegative** [false]: A flag to indicate that the features being searched for are negative. The cube will be inverted prior to searching.
- snrCut** [3.]: The cut-off value for thresholding, in terms of number of σ above the mean.
- flagGrowth** [false]: A flag indicating whether or not to grow the detected objects to a smaller threshold.
- growthCut** [2.]: The smaller threshold using in growing detections. In units of σ above the mean.

***À trous* reconstruction**

flagATrous [true]: A flag indicating whether or not to reconstruct the cube using the *à trous* wavelet reconstruction. See §3.3 for details.

reconDim [3]: The number of dimensions to use in the reconstruction. 1 means reconstruct each spectrum separately, 2 means each channel map is done separately, and 3 means do the whole cube in one go.

scaleMin [1]: The minimum wavelet scale to be used in the reconstruction. A value of 1 means “use all scales”.

snrRecon [4]: The thresholding cutoff used in the reconstruction – only wavelet coefficients this many σ above the mean (or greater) are included in the reconstruction.

filterCode [1]: The code number of the filter to use in the reconstruction. The options are:

- **1:** B₃-spline filter: coefficients = $(\frac{1}{16}, \frac{1}{4}, \frac{3}{8}, \frac{1}{4}, \frac{1}{16})$
- **2:** Triangle filter: coefficients = $(\frac{1}{4}, \frac{1}{2}, \frac{1}{4})$
- **3:** Haar wavelet: coefficients = $(0, \frac{1}{2}, \frac{1}{2})$

FDR method

flagFDR [false]: A flag indicating whether or not to use the False Discovery Rate method in thresholding the pixels.

alphaFDR [0.01]: The α parameter used in the FDR analysis. The average number of false detections, as a fraction of the total number, will be less than α (see §3.5).

Merging detections

minPix [2]: The minimum number of spatial pixels for a single detection to be counted.

minChannels [3]: The minimum number of consecutive channels that must be present in a detection.

flagAdjacent [true]: A flag indicating whether to use the “adjacent pixel” criterion to decide whether to merge objects. If not, the next two parameters are used to determine whether objects are within the necessary thresholds.

threshSpatial [3.]: The maximum allowed minimum spatial separation (in pixels) between two detections for them to be merged into one. Only used if `flagAdjacent = false`.

threshVelocity [7.]: The maximum allowed minimum channel separation between two detections for them to be merged into one.

Other parameters

spectralMethod [peak]: This indicates which method is used to plot the output spectra: `peak` means plot the spectrum containing the detection’s peak

pixel; **sum** means sum the spectra of each detected spatial pixel, and correct for the beam size. Any other choice defaults to **peak**.

spectralUnits [**km/s**]: The user can specify the units of the spectral axis. Assuming the WCS of the FITS file is valid, the spectral axis is transformed into velocity, and put into these units for all output and for calculations such as the integrated flux of a detection.

drawBorders [**true**]: A flag indicating whether borders are to be drawn around the detected objects in the moment maps included in the output (see for example Fig. 1).

verbose [**true**]: A flag indicating whether to print the progress of computationally-intensive algorithms (such as the searching and merging) to screen.

C Example parameter files

This is what a typical parameter file would look like.

```
imageFile      /DATA/SITAR_1/whi550/cubes/H201_abcde_luther_chop.fits
logFile        logfile.txt
outFile        results.txt
spectraFile    spectra.ps
flagSubsection 0
flagOutputRecon 0
flagOutputResid 0
flagBlankPix   1
flagMW         1
minMW          75
maxMW          112
minPix         3
flagGrowth     1
growthCut      1.5
flagATrous     0
scaleMin       1
snrRecon       4
flagFDR        1
alphaFDR       0.1
numPixPSF      20
snrCut         3
threshSpatial  3
threshVelocity 7
```

Note that it is not necessary to include all these parameters in the file, only those that need to be changed from the defaults (as listed in Appendix B), which in this case would be very few. A minimal parameter file might look like:

```
imageFile      /DATA/SITAR_1/whi550/cubes/H201_abcde_luther_chop.fits
flagLog        0
snrRecon       3
snrCut         2.5
minChannels    4
```

This will reconstruct the cube with a lower SNR value than the default, select objects at a lower threshold, with a looser minimum channel requirement, and not keep a log of the intermediate detections.

The following page demonstrates how the parameters are presented to the user, both on the screen at execution time, and in the output and log files. On each line, there is a description on the parameter, the relevant parameter name that is used in the input file (if there is one that the user can enter), and the value of the parameter being used.

Typical presentation of parameters in output and log files:

```

---- Parameters ----
Image to be analysed.....[imageFile]
Intermediate Logfile.....[logFile]
Final Results file.....[outFile]
Spectrum file.....[spectraFile]
Oth Moment Map.....[momentMap]
Detection Map.....[detectionMap]
Saving reconstructed cube?.....[flagoutputrecon]
Saving residuals from reconstruction?..[flagoutputresid]
-----
Searching for Negative features?.....[flagNegative]
Fixing Blank Pixels?.....[flagBlankPix]
Blank Pixel Value.....
Removing Milky Way channels?.....[flagMW]
Milky Way Channels.....[minMW - maxMW]
Beam Size (pixels).....
Removing baselines before search?.....[flagBaseline]
Minimum # Pixels in a detection.....[minPix]
Minimum # Channels in a detection.....[minChannels]
Growing objects after detection?.....[flagGrowth]
Using A Trous reconstruction?.....[flagATrous]
Number of dimensions in reconstruction.....[reconDim]
Minimum scale in reconstruction.....[scaleMin]
SNR Threshold within reconstruction.....[snrRecon]
Filter being used for reconstruction.....[filterCode]
Using FDR analysis?.....[flagFDR]
SNR Threshold.....[snrCut]
Using Adjacent-pixel criterion?.....[flagAdjacent]
Max. velocity separation for merging....[threshVelocity]
Method of spectral plotting.....[spectralMethod]
= input.fits
= duchamp-Logfile.txt
= duchamp-Results.txt
= duchamp-Spectra.ps
= duchamp-MomentMap.ps
= duchamp-DetectionMap.ps
= false
= false
= false
= true
= -8.00061
= true
= 75-112
= 10.1788
= false
= 2
= 3
= false
= true
= 3
= 1
= 4
= 1 (B3 spline function)
= false
= 3
= true
= 7
= peak

```


D Example results file

This is the typical content of an output file, after running *Duchamp* with the parameters illustrated on the previous page.

```

Results of the \duchamp\ source finder: Tue May 23 14:51:38 2006
---- Parameters ----
(... omitted for clarity -- see previous page for examples...)
-----
Total number of detections = 25
-----
Obj#      Name      X      Y      Z      RA      DEC      VEL      w_RA      w_DEC      w_VEL      F_int      F_peak      F1      F2      F3      F4      F5      F6      F7      F8      F9      F10      F11      F12      F13      F14      F15      F16      F17      F18      F19      F20      F21      F22      F23      F24      F25      F26      F27      F28      F29      F30      F31      F32      F33      F34      F35      F36      F37      F38      F39      F40      F41      F42      F43      F44      F45      F46      F47      F48      F49      F50      F51      F52      F53      F54      F55      F56      F57      F58      F59      F60      F61      F62      F63      F64      F65      F66      F67      F68      F69      F70      F71      F72      F73      F74      F75      F76      F77      F78      F79      F80      F81      F82      F83      F84      F85      F86      F87      F88      F89      F90      F91      F92      F93      F94      F95      F96      F97      F98      F99      F100      F101      F102      F103      F104      F105      F106      F107      F108      F109      F110      F111      F112      F113      F114      F115      F116      F117      F118      F119      F120      F121      F122      F123      F124      F125      F126      F127      F128      F129      F130      F131      F132      F133      F134      F135      F136      F137      F138      F139      F140      F141      F142      F143      F144      F145      F146      F147      F148      F149      F150      F151      F152      F153      F154      F155      F156      F157      F158      F159      F160      F161      F162      F163      F164      F165      F166      F167      F168      F169      F170      F171      F172      F173      F174      F175      F176      F177      F178      F179      F180      F181      F182      F183      F184      F185      F186      F187      F188      F189      F190      F191      F192      F193      F194      F195      F196      F197      F198      F199      F200      F201      F202      F203      F204      F205      F206      F207      F208      F209      F210      F211      F212      F213      F214      F215      F216      F217      F218      F219      F220      F221      F222      F223      F224      F225      F226      F227      F228      F229      F230      F231      F232      F233      F234      F235      F236      F237      F238      F239      F240      F241      F242      F243      F244      F245      F246      F247      F248      F249      F250      F251      F252      F253      F254      F255      F256      F257      F258      F259      F260      F261      F262      F263      F264      F265      F266      F267      F268      F269      F270      F271      F272      F273      F274      F275      F276      F277      F278      F279      F280      F281      F282      F283      F284      F285      F286      F287      F288      F289      F290      F291      F292      F293      F294      F295      F296      F297      F298      F299      F300      F301      F302      F303      F304      F305      F306      F307      F308      F309      F310      F311      F312      F313      F314      F315      F316      F317      F318      F319      F320      F321      F322      F323      F324      F325      F326      F327      F328      F329      F330      F331      F332      F333      F334      F335      F336      F337      F338      F339      F340      F341      F342      F343      F344      F345      F346      F347      F348      F349      F350      F351      F352      F353      F354      F355      F356      F357      F358      F359      F360      F361      F362      F363      F364      F365      F366      F367      F368      F369      F370      F371      F372      F373      F374      F375      F376      F377      F378      F379      F380      F381      F382      F383      F384      F385      F386      F387      F388      F389      F390      F391      F392      F393      F394      F395      F396      F397      F398      F399      F400      F401      F402      F403      F404      F405      F406      F407      F408      F409      F410      F411      F412      F413      F414      F415      F416      F417      F418      F419      F420      F421      F422      F423      F424      F425      F426      F427      F428      F429      F430      F431      F432      F433      F434      F435      F436      F437      F438      F439      F440      F441      F442      F443      F444      F445      F446      F447      F448      F449      F450      F451      F452      F453      F454      F455      F456      F457      F458      F459      F460      F461      F462      F463      F464      F465      F466      F467      F468      F469      F470      F471      F472      F473      F474      F475      F476      F477      F478      F479      F480      F481      F482      F483      F484      F485      F486      F487      F488      F489      F490      F491      F492      F493      F494      F495      F496      F497      F498      F499      F500      F501      F502      F503      F504      F505      F506      F507      F508      F509      F510      F511      F512      F513      F514      F515      F516      F517      F518      F519      F520      F521      F522      F523      F524      F525      F526      F527      F528      F529      F530      F531      F532      F533      F534      F535      F536      F537      F538      F539      F540      F541      F542      F543      F544      F545      F546      F547      F548      F549      F550      F551      F552      F553      F554      F555      F556      F557      F558      F559      F560      F561      F562      F563      F564      F565      F566      F567      F568      F569      F570      F571      F572      F573      F574      F575      F576      F577      F578      F579      F580      F581      F582      F583      F584      F585      F586      F587      F588      F589      F590      F591      F592      F593      F594      F595      F596      F597      F598      F599      F600      F601      F602      F603      F604      F605      F606      F607      F608      F609      F610      F611      F612      F613      F614      F615      F616      F617      F618      F619      F620      F621      F622      F623      F624      F625      F626      F627      F628      F629      F630      F631      F632      F633      F634      F635      F636      F637      F638      F639      F640      F641      F642      F643      F644      F645      F646      F647      F648      F649      F650      F651      F652      F653      F654      F655      F656      F657      F658      F659      F660      F661      F662      F663      F664      F665      F666      F667      F668      F669      F670      F671      F672      F673      F674      F675      F676      F677      F678      F679      F680      F681      F682      F683      F684      F685      F686      F687      F688      F689      F690      F691      F692      F693      F694      F695      F696      F697      F698      F699      F700      F701      F702      F703      F704      F705      F706      F707      F708      F709      F710      F711      F712      F713      F714      F715      F716      F717      F718      F719      F720      F721      F722      F723      F724      F725      F726      F727      F728      F729      F730      F731      F732      F733      F734      F735      F736      F737      F738      F739      F740      F741      F742      F743      F744      F745      F746      F747      F748      F749      F750      F751      F752      F753      F754      F755      F756      F757      F758      F759      F760      F761      F762      F763      F764      F765      F766      F767      F768      F769      F770      F771      F772      F773      F774      F775      F776      F777      F778      F779      F780      F781      F782      F783      F784      F785      F786      F787      F788      F789      F790      F791      F792      F793      F794      F795      F796      F797      F798      F799      F800      F801      F802      F803      F804      F805      F806      F807      F808      F809      F810      F811      F812      F813      F814      F815      F816      F817      F818      F819      F820      F821      F822      F823      F824      F825      F826      F827      F828      F829      F830      F831      F832      F833      F834      F835      F836      F837      F838      F839      F840      F841      F842      F843      F844      F845      F846      F847      F848      F849      F850      F851      F852      F853      F854      F855      F856      F857      F858      F859      F860      F861      F862      F863      F864      F865      F866      F867      F868      F869      F870      F871      F872      F873      F874      F875      F876      F877      F878      F879      F880      F881      F882      F883      F884      F885      F886      F887      F888      F889      F890      F891      F892      F893      F894      F895      F896      F897      F898      F899      F900      F901      F902      F903      F904      F905      F906      F907      F908      F909      F910      F911      F912      F913      F914      F915      F916      F917      F918      F919      F920      F921      F922      F923      F924      F925      F926      F927      F928      F929      F930      F931      F932      F933      F934      F935      F936      F937      F938      F939      F940      F941      F942      F943      F944      F945      F946      F947      F948      F949      F950      F951      F952      F953      F954      F955      F956      F957      F958      F959      F960      F961      F962      F963      F964      F965      F966      F967      F968      F969      F970      F971      F972      F973      F974      F975      F976      F977      F978      F979      F980      F981      F982      F983      F984      F985      F986      F987      F988      F989      F990      F991      F992      F993      F994      F995      F996      F997      F998      F999      F1000      F1001      F1002      F1003      F1004      F1005      F1006      F1007      F1008      F1009      F1010      F1011      F1012      F1013      F1014      F1015      F1016      F1017      F1018      F1019      F1020      F1021      F1022      F1023      F1024      F1025      F1026      F1027      F1028      F1029      F1030      F1031      F1032      F1033      F1034      F1035      F1036      F1037      F1038      F1039      F1040      F1041      F1042      F1043      F1044      F1045      F1046      F1047      F1048      F1049      F1050      F1051      F1052      F1053      F1054      F1055      F1056      F1057      F1058      F1059      F1060      F1061      F1062      F1063      F1064      F1065      F1066      F1067      F1068      F1069      F1070      F1071      F1072      F1073      F1074      F1075      F1076      F1077      F1078      F1079      F1080      F1081      F1082      F1083      F1084      F1085      F1086      F1087      F1088      F1089      F1090      F1091      F1092      F1093      F1094      F1095      F1096      F1097      F1098      F1099      F1100      F1101      F1102      F1103      F1104      F1105      F1106      F1107      F1108      F1109      F1110      F1111      F1112      F1113      F1114      F1115      F1116      F1117      F1118      F1119      F1120      F1121      F1122      F1123      F1124      F1125      F1126      F1127      F1128      F1129      F1130      F1131      F1132      F1133      F1134      F1135      F1136      F1137      F1138      F1139      F1140      F1141      F1142      F1143      F1144      F1145      F1146      F1147      F1148      F1149      F1150      F1151      F1152      F1153      F1154      F1155      F1156      F1157      F1158      F1159      F1160      F1161      F1162      F1163      F1164      F1165      F1166      F1167      F1168      F1169      F1170      F1171      F1172      F1173      F1174      F1175      F1176      F1177      F1178      F1179      F1180      F1181      F1182      F1183      F1184      F1185      F1186      F1187      F1188      F1189      F1190      F1191      F1192      F1193      F1194      F1195      F1196      F1197      F1198      F1199      F1200      F1201      F1202      F1203      F1204      F1205      F1206      F1207      F1208      F1209      F1210      F1211      F1212      F1213      F1214      F1215      F1216      F1217      F1218      F1219      F1220      F1221      F1222      F1223      F1224      F1225      F1226      F1227      F1228      F1229      F1230      F1231      F1232      F1233      F1234      F1235      F1236      F1237      F1238      F1239      F1240      F1241      F1242      F1243      F1244      F1245      F1246      F1247      F1248      F1249      F1250      F1251      F1252      F1253      F1254      F1255      F1256      F1257      F1258      F1259      F1260      F1261      F1262      F1263      F1264      F1265      F1266      F1267      F1268      F1269      F1270      F1271      F1272      F1273      F1274      F1275      F1276      F1277      F1278      F1279      F1280      F1281      F1282      F1283      F1284      F1285      F1286      F1287      F1288      F1289      F1290      F1291      F1292      F1293      F1294      F1295      F1296      F1297      F1298      F1299      F1300      F1301      F1302      F1303      F1304      F1305      F1306      F1307      F1308      F1309      F1310      F1311      F1312      F1313      F1314      F1315      F1316      F1317      F1318      F1319      F1320      F1321      F1322      F1323      F1324      F1325      F1326      F1327      F1328      F1329      F1330      F1331      F1332      F1333      F1334      F1335      F1336      F1337      F1338      F1339      F1340      F1341      F1342      F1343      F1344      F1345      F1346      F1347      F1348      F1349      F1350      F1351      F1352      F1353      F1354      F1355      F1356      F1357      F1358      F1359      F1360      F1361      F1362      F1363      F1364      F1365      F1366      F1367      F1368      F1369      F1370      F1371      F1372      F1373      F1374      F1375      F1376      F1377      F1378      F1379      F1380      F1381      F1382      F1383      F1384      F1385      F1386      F1387      F1388      F1389      F1390      F1391      F1392      F1393      F1394      F1395      F1396      F1397      F1398      F1399      F1400      F1401      F1402      F1403      F1404      F1405      F1406      F1407      F1408      F1409      F1410      F1411      F1412      F1413      F1414      F1415      F1416      F1417      F1418      F1419      F1420      F1421      F1422      F1423      F1424      F1425      F1426      F1427      F1428      F1429      F1430      F1431      F1432      F1433      F1434      F1435      F1436      F1437      F1438      F1439      F1440      F1441      F1442      F1443      F1444      F1445      F1446      F1447      F1448      F1449      F1450      F1451      F1452      F1453      F1454      F1455      F1456      F1457      F1458      F1459      F1460      F1461      F1462      F1463      F1464      F1465      F1466      F1467      F1468      F1469      F1470      F1471      F1472      F1473      F1474      F1475      F1476      F1477      F1478      F1479      F1480      F1481      F1482      F1483      F1484      F1485      F1486      F1487      F1488      F1489      F1490      F1491      F1492      F1493      F1494      F1495      F1496      F1497      F1498      F1499      F1500      F1501      F1502      F1503      F1504      F1505      F1506      F1507      F1508      F1509      F1510      F1511      F1512      F1513      F1514      F1515      F1516      F1517      F1518      F1519      F1520      F1521      F1522      F1523      F1524      F1525      F1526      F1527      F1528      F1529      F1530      F1531      F1532      F1533      F1534      F1535      F1536      F1537      F1538      F1539      F1540      F1541      F1542      F1543      F1544      F1545      F1546      F1547      F1548      F1549      F1550      F1551      F1552      F1553      F1554      F1555      F1556      F1557      F1558      F1559      F1560      F1561      F1562      F1563      F1564      F1565      F1566      F1567      F1568      F1569      F1570      F1571      F1572      F1573      F1574      F1575      F1576      F1577      F1578      F1579      F1580      F1581      F1582      F1583      F1584      F1585      F1586      F1587      F1588      F1589      F1590      F1591      F1592      F1593      F1594      F1595      F1596      F1597      F1598      F1599      F1600      F1601      F1602      F1603      F1604      F1605      F1606      F1607      F1608      F1609      F1610      F1611      F1612      F1613      F1614      F1615      F1616      F1617      F1618      F1619      F1620      F1621      F1622      F1623      F1624      F1625      F1626      F1627      F1628      F1629      F1630      F1631      F1632      F1633      F1634      F1635      F1636      F1637      F1638      F1639      F1640      F1641      F1642      F1643      F1644      F1645      F1646      F1647      F1648      F1649      F1650      F1651      F1652      F1653      F1654      F1655      F1656      F1657      F1658      F1659      F1660      F1661      F1662      F1663      F1664      F1665      F1666      F1667      F1668      F1669      F1670      F1671      F1672      F1673      F1674      F1675      F1676      F1677      F1678      F1679      F1680      F1681      F1682      F1683      F1684      F1685      F1686      F1687      F1688      F1689      F1690      F1691      F1692      F1693      F1694      F1695      F1696      F1697      F1698      F1699      F1700      F1701      F1702      F1703      F1704      F1705      F1706      F1707      F1708      F1709      F1710      F1711      F1712      F1713      F1714      F1715      F1716      F1717      F1718      F1719      F1720      F1721      F1722      F1723      F1724      F1725      F1726      F1727      F1728      F1729      F1730      F1731      F1732      F1733      F1734      F1735      F1736      F1737      F1738      F1739      F1740      F1741      F1742      F1743      F1744      F1745      F1746      F1747      F1748      F1749      F1750      F1751      F1752      F1753      F1754      F1755      F1756      F1757      F1758      F1759      F1760      F1761      F1762      F1763      F1764      F1765      F1766      F1767      F1768      F1769      F1770      F1771      F1772      F1773      F1774      F1775      F1776      F1777      F1778      F1779      F1780      F1781      F1782      F1783      F1784      F1785      F1786      F1787      F1788      F1789      F1790      F1791      F1792      F1793      F1794      F1795      F1796      F1797      F1798      F1799      F1800      F1801      F1802      F1803      F1804      F1805      F1806      F1807      F1808      F1809      F1810      F1811      F1812      F1813      F1814      F1815      F1816      F1817      F1818      F1819      F1820      F1821      F1822      F1823      F1824      F1825      F1826      F1827      F1828      F1829      F1830      F1831      F1832      F1833      F1834      F1835      F1836      F1837      F1838      F1839      F1840      F1841      F1842      F1843      F1844      F1845      F1846      F1847      F1848      F1849      F1850      F1851      F1852      F1853      F1854      F1855      F1856      F1857      F1858      F1859      F1860      F1861      F1862      F1863      F1864      F1865      F1866      F1867      F1868      F1869      F1870      F1871      F1872      F1873      F1874      F1875      F1876      F1877      F1878      F1879      F1880      F1881      F1882      F1883      F1884      F1885      F1886      F1887      F1888      F1889      F1890      F1891      F1892      F1893      F1894      F1895      F1896      F1897      F1898      F1899      F1900      F1901      F1902      F1903      F1904      F1905      F1906      F1907      F1908      F1909      F1910      F1911      F1912      F1913      F1914      F1915      F1916      F1917      F1918      F1919      F1920      F1921      F1922      F1923      F1924      F1925      F1926      F1927      F1928      F1929      F1930      F1931      F1932      F1933      F1934      F1935      F1936      F1937      F1938      F1939      F1940      F1941      F1942      F1943      F1944      F1945      F1946      F1947      F1948      F1949      F1950      F1951      F1952      F1953      F1954      F1955      F1956      F1957      F1958      F1959      F1960      F1961      F1962      F1963      F1964      F1965      F1966      F1967      F1968      F1969      F1970      F1971      F1972      F1973      F1974      F1975      F1976      F1977      F1978      F1979      F1980      F1981      F1982      F1983      F1984      F1985      F1986      F1987      F1988      F1989      F1990      F1991      F1992      F1993      F1994      F1995      F1996      F1997      F1998      F1999      F2000      F2001      F2002      F2003      F2004      F2005      F2006      F2007      F2008      F2009      F2010      F2011      F2012      F2013      F2014      F2015      F2016      F2017      F2018      F2019      F2020      F2021      F2022      F2023      F2024      F2025      F2026      F2027      F2028      F2029      F2030      F2031      F2032      F2033      F2034      F2035      F2036      F2037      F2038      F2039      F2040      F2041      F2042      F2043      F2044      F2045      F2046      F2047      F2048      F2049      F2050      F2051      F2052      F2053      F2054      F2055      F2056      F2057      F2058      F2059      F2060      F2061      F2062      F2063      F2064      F2065      F2066      F2067      F2068      F2069      F2070      F2071      F2072      F2073      F2074      F2075      F2076      F2077      F2078      F2079      F2080      F2081      F2082      F2083      F2084      F2085      F2086      F2087      F2088      F2089      F2090      F2091      F2092      F2093      F2094      F2095      F2096      F2097      F2098      F2099      F2100      F2101      F2102      F2103      F2104      F2105      F2106      F2107      F2108      F2109      F2110      F2111      F2112      F2113      F2114      F2115      F2116      F2117      F2118      F2119      F2120      F2121      F2122      F2123      F2124      F2125      F2126      F2127      F2128      F2129      F2130      F2131      F2132      F2133      F2134      F2135      F2136      F2137      F2138      F2139      F2140      F2141      F2142      F2143      F2144      F2145      F2146      F2147      F2148      F2149      F2150      F2151      F2152      F2153      F2154      F2155      F2156      F2157      F2158      F2159      F2160      F2161      F2162      F2163      F2164      F2165      F2166      F2167      F2168      F2169      F2170      F2171      F2172      F2173      F2174      F2175      F2176      F2177      F2178      F2179      F2180      F2181      F2182      F2183      F2184      F2185      F2186      F2187      F2188      F2189      F2190      F2191      F2192      F2193      F2194      F2195      F2196      F2197      F2198      F21
```

E Example VOTable output

This is part of the VOTable, in XML format, corresponding to the output file in Appendix D (the indentation has been removed to make it fit on the page).

```

<?xml version="1.0"?>
<VOTABLE version="1.1" xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance"
  xsi:noNamespaceSchemaLocation="http://www.ivoa.net/xml/VOTable/VOTable/v1.1">
<COOSYS ID="J2000" equinox="J2000." epoch="J2000." system="eq_FK5"/>
<RESOURCE name="Duchamp Output">
<TABLE name="Detections">
<DESCRIPTION>Detected sources and parameters from running the Duchamp source finder.</DESCRIPTION>
<PARAM name="FITS file" datatype="char" ucd="meta.file;meta.fits" value="/DATA/SITAR_1/whi550/cubes/H201_abcd_luther_chop.fits"/>
<PARAM name="Threshold" datatype="float" ucd="stat.snr" value="2.5">
<PARAM name="ATrous note" datatype="char" ucd="meta.note" value="The a trous reconstruction method was used, with the following parameters.">
<PARAM name="ATrous Dimension" datatype="int" ucd="meta.code;stat" value="3">
<PARAM name="ATrous Cut" datatype="float" ucd="stat.snr" value="4">
<PARAM name="ATrous Minimum Scale" datatype="int" ucd="stat.param" value="1">
<PARAM name="ATrous Filter" datatype="char" ucd="meta.code;stat" value="B3 spline function">
<FIELD name="ID" ID="col1" ucd="meta.id" datatype="int" width="4"/>
<FIELD name="Name" ID="col2" ucd="meta.id;meta.main" datatype="char" arraysize="14"/>
<FIELD name="RA" ID="col3" ucd="pos.eq.ra;meta.main" ref="J2000" datatype="float" width="10" precision="6" unit="deg"/>
<FIELD name="Dec" ID="col4" ucd="pos.eq.dec;meta.main" ref="J2000" datatype="float" width="10" precision="6" unit="deg"/>
<FIELD name="w_RA" ID="col3" ucd="phys.angSize;pos.eq.ra" ref="J2000" datatype="float" width="7" precision="2" unit="arcmin"/>
<FIELD name="w_Dec" ID="col4" ucd="phys.angSize;pos.eq.dec" ref="J2000" datatype="float" width="7" precision="2" unit="arcmin"/>
<FIELD name="Vel" ID="col4" ucd="phys.veloc;src.dopplerVeloc" datatype="float" width="9" precision="3" unit="km/s"/>
<FIELD name="w_Vel" ID="col4" ucd="phys.veloc;src.dopplerVeloc;spect.line.width" datatype="float" width="8" precision="3" unit="km/s"/>
<FIELD name="Integrated_Flux" ID="col4" ucd="phys.flux;spect.line.intensity" datatype="float" width="10" precision="3" unit="km/s"/>
<DATA>
<TABLEDATA>
<TR>
<TD> 1</TD><TD> J0609-2200</TD><TD> 92.410416</TD><TD>-22.013390</TD><TD> 48.50</TD><TD> 39.42</TD><TD> 213.061</TD><TD> 65.957</TD><TD> 17.572</TD>
</TR>
<TR>
<TD> 2</TD><TD> J0608-2605</TD><TD> 92.042633</TD><TD>-26.085157</TD><TD> 44.47</TD><TD> 233.119</TD><TD> 39.574</TD><TD> 4.144</TD>
</TR>
<TR>
<TD> 3</TD><TD> J0606-2724</TD><TD> 91.637840</TD><TD>-27.412022</TD><TD> 52.48</TD><TD> 302.213</TD><TD> 39.574</TD><TD> 17.066</TD>
</TR>
(... table truncated for clarity ...)
</TABLEDATA>
</DATA>
</TABLE>
</RESOURCE>
</VOTABLE>

```

F Example Karma Annotation File output

This is the format of the Karma Annotation file, showing the locations of the detected objects. This can be loaded by the plotting tools of the Karma package (for instance, `kvis`) as an overlay on the FITS file.

```
# Duchamp Source Finder results for
# cube /DATA/SITAR_1/whi550/cubes/H201_abcde_luther_chop.fits
COLOR RED
COORD W
CIRCLE 92.3376 -21.9475 0.403992
TEXT 92.3376 -21.9475 1
CIRCLE 91.9676 -26.0193 0.37034
TEXT 91.9676 -26.0193 2
CIRCLE 91.5621 -27.3459 0.437109
TEXT 91.5621 -27.3459 3
CIRCLE 92.8285 -21.6344 0.269914
TEXT 92.8285 -21.6344 4
CIRCLE 90.1381 -28.9838 0.234179
TEXT 90.1381 -28.9838 5
CIRCLE 89.72 -26.6513 0.132743
TEXT 89.72 -26.6513 6
CIRCLE 94.2743 -27.4003 0.195175
TEXT 94.2743 -27.4003 7
CIRCLE 92.2739 -21.6941 0.134538
TEXT 92.2739 -21.6941 8
CIRCLE 89.7133 -25.4259 0.232252
TEXT 89.7133 -25.4259 9
CIRCLE 90.2206 -21.6993 0.266247
TEXT 90.2206 -21.6993 10
CIRCLE 93.8581 -26.5766 0.163153
TEXT 93.8581 -26.5766 11
CIRCLE 91.176 -26.1064 0.234356
TEXT 91.176 -26.1064 12
CIRCLE 90.2844 -23.6716 0.299509
TEXT 90.2844 -23.6716 13
CIRCLE 93.8774 -22.581 0.130925
TEXT 93.8774 -22.581 14
CIRCLE 94.3882 -23.0934 0.137108
TEXT 94.3882 -23.0934 15
CIRCLE 93.0491 -21.8223 0.202928
TEXT 93.0491 -21.8223 16
CIRCLE 94.0685 -21.5603 0.168456
TEXT 94.0685 -21.5603 17
CIRCLE 86.0568 -27.6095 0.101113
TEXT 86.0568 -27.6095 18
CIRCLE 88.7932 -29.9453 0.202624
TEXT 88.7932 -29.9453 19
```

G Robust statistics for a Normal distribution

The Normal, or Gaussian, distribution for mean μ and standard deviation σ can be written as

$$f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-(x-\mu)^2/2\sigma^2}.$$

When one has a purely Gaussian signal, it is straightforward to estimate σ by calculating the standard deviation (or rms) of the data. However, if there is a small amount of signal present on top of Gaussian noise, and one wants to estimate the σ for the noise, the presence of the large values from the signal can bias the estimator to higher values.

An alternative way is to use the median (m) and median absolute deviation from the median (s) to estimate μ and σ . The median is the middle of the distribution, defined for a continuous distribution by

$$\int_{-\infty}^m f(x)dx = \int_m^{\infty} f(x)dx.$$

From symmetry, we quickly see that for the continuous Normal distribution, $m = \mu$. We consider the case henceforth of $\mu = 0$, without loss of generality.

To find s , we find the distribution of the absolute deviation from the median, and then find the median of that distribution. This distribution is given by

$$\begin{aligned} g(x) &= \text{distribution of } |x| \\ &= f(x) + f(-x), \quad x \geq 0 \\ &= \sqrt{\frac{2}{\pi\sigma^2}} e^{-x^2/2\sigma^2}, \quad x \geq 0. \end{aligned}$$

So, the median absolute deviation from the median, s , is given by

$$\int_0^s g(x)dx = \int_s^{\infty} g(x)dx.$$

Now, $\int_0^{\infty} e^{-x^2/2\sigma^2} dx = \sqrt{\pi\sigma^2/2}$, and so $\int_s^{\infty} e^{-x^2/2\sigma^2} dx = \sqrt{\pi\sigma^2/2} - \int_0^s e^{-x^2/2\sigma^2} dx$. Hence, to find s we simply solve the following equation (setting $\sigma = 1$ for simplicity – equivalent to stating x and s in units of σ):

$$\int_0^s e^{-x^2/2} dx - \sqrt{\pi/8} = 0.$$

This is hard to solve analytically (no nice analytic solution exists for the finite integral that I'm aware of), but straightforward to solve numerically, yielding the value of $s = 0.6744888$. Thus, to estimate σ for a Normally distributed data set, one can calculate s , then divide by 0.6744888 (or multiply by 1.4826042) to obtain the correct estimator.

Note that this is different to solutions quoted elsewhere, specifically in [Meyer et al. \(2004\)](#), where the same robust estimator is used but with an incorrect conversion to standard deviation – they assume $\sigma = s\sqrt{\pi/2}$. This, in fact, is the conversion used to convert the *mean* absolute deviation from the mean to the standard deviation. This means that the cube noise in the HIPASS catalogue (their parameter Rms_{cube}) should be 18% larger than quoted.

H How Gaussian noise changes with wavelet scale.

The key element in the wavelet reconstruction of an array is the thresholding of the individual wavelet coefficient arrays. This is usually done by choosing a level to be some number of standard deviations above the mean value.

However, since the wavelet arrays are produced by convolving the input array by an increasingly large filter, the pixels in the coefficient arrays become increasingly correlated as the scale of the filter increases. This results in the measured standard deviation from a given coefficient array decreasing with increasing scale. To calculate this, we need to take into account how many other pixels each pixel in the convolved array depends on.

To demonstrate, suppose we have a 1-D array with N pixel values given by F_i , $i = 1, \dots, N$, and we convolve it with the B₃-spline filter, defined by the set of coefficients $\{1/16, 1/4, 3/8, 1/4, 1/16\}$. The flux of the i th pixel in the convolved array will be

$$F'_i = \frac{1}{16}F_{i-2} + \frac{1}{4}F_{i-1} + \frac{3}{8}F_i + \frac{1}{4}F_{i+1} + \frac{1}{16}F_{i+2}$$

and the flux of the corresponding pixel in the wavelet array will be

$$W'_i = F_i - F'_i = \frac{-1}{16}F_{i-2} - \frac{1}{4}F_{i-1} + \frac{5}{8}F_i - \frac{1}{4}F_{i+1} - \frac{1}{16}F_{i+2}$$

Now, assuming each pixel has the same standard deviation $\sigma_i = \sigma$, we can work out the standard deviation for the wavelet array:

$$\sigma'_i = \sigma \sqrt{\left(\frac{1}{16}\right)^2 + \left(\frac{1}{4}\right)^2 + \left(\frac{5}{8}\right)^2 + \left(\frac{1}{4}\right)^2 + \left(\frac{1}{16}\right)^2} = 0.72349 \sigma$$

Thus, the first scale wavelet coefficient array will have a standard deviation of 72.3% of the input array. This procedure can be followed to calculate the necessary values for all scales, dimensions and filters used by *Duchamp*.

Calculating these values is clearly a critical step in performing the reconstruction. [Starck & Murtagh \(2002\)](#) did so by simulating data sets with Gaussian noise, taking the wavelet transform, and measuring the value of σ for each scale. We take a different approach, by calculating the scaling factors directly from the filter coefficients by taking the wavelet transform of an array made up of a 1 in the central pixel and 0s everywhere else. The scaling value is then derived by taking the square root of the sum (in quadrature) of all the wavelet coefficient values at each scale. We give the scaling factors for the three filters available to *Duchamp* on the following page. These values are hard-coded into *Duchamp*, so no on-the-fly calculation of them is necessary.

Memory limitations prevent us from calculating factors for large scales, particularly for the three-dimensional case (hence the – symbols in the tables). To calculate factors for higher scales than those available, we note the following relationships apply for large scales to a sufficient level of precision:

- 1-D: factor(scale i) = factor(scale $i - 1$)/ $\sqrt{2}$.
- 2-D: factor(scale i) = factor(scale $i - 1$)/2.
- 1-D: factor(scale i) = factor(scale $i - 1$)/ $\sqrt{8}$.

- **B₃-Spline Function:** $\{1/16, 1/4, 3/8, 1/4, 1/16\}$

Scale	1 dimension	2 dimension	3 dimension
1	0.723489806	0.890796310	0.956543592
2	0.285450405	0.200663851	0.120336499
3	0.177947535	0.0855075048	0.0349500154
4	0.122223156	0.0412474444	0.0118164242
5	0.0858113122	0.0204249666	0.00413233507
6	0.0605703043	0.0101897592	0.00145703714
7	0.0428107206	0.00509204670	0.000514791120
8	0.0302684024	0.00254566946	–
9	0.0214024008	0.00127279050	–
10	0.0151336781	0.000636389722	–
11	0.0107011079	0.000318194170	–
12	0.00756682272	–	–
13	0.00535055108	–	–

- **Triangle Function:** $\{1/4, 1/2, 1/4\}$

Scale	1 dimension	2 dimension	3 dimension
1	0.612372436	0.800390530	0.895954449
2	0.330718914	0.272878894	0.192033014
3	0.211947812	0.119779282	0.0576484078
4	0.145740298	0.0577664785	0.0194912393
5	0.102310944	0.0286163283	0.00681278387
6	0.0722128185	0.0142747506	0.00240175885
7	0.0510388224	0.00713319703	0.000848538128
8	0.0360857673	0.00356607618	0.000299949455
9	0.0255157615	0.00178297280	–
10	0.0180422389	0.000891478237	–
11	0.0127577667	0.000445738098	–
12	0.00902109930	0.000222868922	–
13	0.00637887978	–	–

- **Haar Wavelet:** $\{0, 1/2, 1/2\}$

Scale	1 dimension	2 dimension	3 dimension
1	0.707167810	0.433012702	0.935414347
2	0.500000000	0.216506351	0.330718914
3	0.353553391	0.108253175	0.116926793
4	0.250000000	0.0541265877	0.0413398642
5	0.176776695	0.0270632939	0.0146158492
6	0.125000000	0.0135316469	0.00516748303